

Lectures on Contest Mathematics

RS1 Contest Supplement for AMC12 and AIME

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Zuming Feng
Phillips Exeter Academy and IDEA Math
zfeng@exeter.edu

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“Cogito ergo Sum” – “I think, therefore I am”

René Descartes (1596-1650)

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Contents

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Algebra	1
1.1 Practical examples with geometric series	1
1.1.1 Finance	1
1.1.2 Bouncing balls	2
1.2 (Infinite) geometric series	4
1.3 Operations rules with logarithm	6
1.4 Computations with logarithm	9
1.5 Recursions	10
1.6 Quadratic equations	13
1.7 Absolute value functions	14
1.7.1 Absolute value functions	14
1.7.2 Mixed exercises	14
1.8 Polynomial and its roots	16
1.9 Algebra 3.1	18
1.10 Algebra 3.2	19
1.11 Algebra 3.3	20
Combinatorics	21
2.1 Basic counting strategies 1	21
2.1.1 Addition and multiplication principles	21
2.1.2 Permutations	21
2.1.3 Combinations	22
2.1.4 Exercises	23
2.2 Basic counting strategies 2	24
2.2.1 Bijections	24
2.2.2 Exercises	25
2.3 Basic counting strategies 3	26
2.3.1 Geometric probabilities	26
2.3.2 Recursions	26
2.4 Practices with basic counting strategies	28

3	Geometry	31
3.1	Revisiting special angles (part 1)	31
3.2	Revisiting special angles (part 2)	33
3.3	Revisiting similarity	34
4	Practice tests	35
4.1	More advanced level problems from EMC ² 2010	35
4.2	More advanced level problems from EMC ² 2011	37