

Lectures on Contest Mathematics

US2 – Comprehensive Introduction to Contest Algebra and Geometry

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Yunhua Xu and Zuming Feng
Phillips Exeter Academy and IDEA Math
zfeng@exeter.edu

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“Cogito ergo Sum” – “I think, therefore I am”

René Descartes (1596-1650)

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